

Focal mechanism determination of induced microearthquakes in an oil field using full waveforms from shallow and deep seismic networks

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ABSTRACT

A new, relatively high frequency, full waveform matching method was used to study the focal mechanisms of small, local earthquakes induced in an oil field, which are monitored by a sparse near-surface network and a deep borehole network. The determined source properties are helpful for understanding the local stress regime in this field. During the waveform inversion, we maximize both the phase and amplitude matching between the observed and modeled waveforms. We also use the polarities of the first P-wave arrivals and the average S/P amplitude ratios to better constrain the matching. An objective function is constructed to include all four criteria. For different hypocenters and source types, comprehensive synthetic tests showed that our method is robust enough to determine the focal mechanisms

under the current array geometries, even when there is considerable velocity inaccuracy. The application to several tens of induced microseismic events showed satisfactory waveform matching between modeled and observed seismograms. Most of the events have a strike direction parallel with the major north-east-southwest faults in the region, and some events trend parallel with the northwest-southeast conjugate faults. The results are consistent with the in situ well breakout measurements and the current knowledge on the stress direction of this region. The source mechanisms of the studied events, together with the hypocenter distribution, indicate that the microearthquakes are caused by the reactivation of preexisting faults. We observed that the faulting mechanism varies with depth, from strike-slip dominance at shallower depth to normal faulting dominance at greater depth.

INTRODUCTION

Induced seismicity is a common phenomenon in oil/gas reservoirs accompanying changes in internal stress due to water injection or water/oil/gas extraction, etc. (e.g., Suckale, 2010; Maxwell et al., 2010). For example, the gas/oil extraction can cause reservoir compaction and reactivate preexisting faults and induce microearthquakes (e.g., Chan and Zoback, 2007; Miyazawa et al., 2008; Sarkar et al., 2008), or injection of water can cause the decrease of effective stress and slippage along preexisting faults (Grasso, 1992). The reactivation of preexisting faults is very likely responsible for the sheared casings of production wells in some fields (Maury et al., 1992) or is a serious source of wellbore instability during drillings (Willson et al., 1998; Zoback and Zinke, 2002). The hydraulic fracturing activities in an enhanced geothermal system or in shale gas extraction can also result in crack openings and closures and induce

microseismicity (Baig and Urbancic, 2010). Through the studying of locations and source characteristics (e.g., focal mechanism) of the induced seismicity over an extended time period, temporal and spatial changes of the stress in the fields may be reconstructed; this can help to understand the intrinsic response of geological formations to the stress disturbance.

Microearthquakes usually have small magnitudes and are generally recorded at sparse local stations. As a result, it is difficult to obtain enough seismic waveforms with high signal-to-noise ratio for picking the polarity information of first P-wave arrivals. Therefore, it is challenging to use only the P-wave polarity information (even when adding S/P amplitude ratios) as used in conventional methods to constrain the focal mechanisms of the induced earthquakes (e.g., Hardebeck and Shearer, 2002, 2003), especially when there are only a limited number of stations. Waveform matching has been used to determine earthquake focal mechanisms on a regional

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and global scale using low frequency waveform information (e.g., Šílený et al., 1992; Zhao and Helmberger, 1994; Tan and Helmberger, 2007). Šílený et al. (1992) use waveform matching to determine the best-fit focal mechanism, source time function and source depth. Zhao and Helmberger (1994) allowed time-shift in the synthetic seismograms to account for the imperfect Green's functions when matching the synthetic with observed seismograms. Tan and Helmberger (2007) match the direct P-arrival phases (the first whole cycle after initial P-arrival) between synthetic and observed seismograms to determine the focal mechanisms. However, in the case of induced seismicity, waveforms usually have higher frequencies. There have been many studies on determining the focal mechanism of the induced seismicity in the cases of enhanced geothermal system development, mining, and hydraulic fracturing. Godano et al. (2011) use the direct amplitudes of P, SV, and SH to study the focal mechanisms of induced microearthquakes in a geothermal site using full-space homogeneous velocity models. Nolen-Hoeksema et al. (2001) use the first half cycle after the first arrivals from the observed seismograms and synthetics from full-space Green's functions to determine the focal mechanisms of several hydraulic fracture events. Julian et al. (2007) use first arrival polarities and amplitude ratios from 16 three-component borehole stations and 14 three-component surface stations to determine the full moment tensors of the induced events and studied the volume change accompanying the geothermal process. High frequency waveform matching, in addition to polarity information, has been used to determine the focal mechanisms of induced earthquakes in a mine with a dense network of 20 stations (Julià and Nyblade, 2009). Julià and Nyblade (2009) use a full-space homogeneous model to calculate the Green's functions, and they performed the focal mechanism inversion in the frequency domain without phase information in a least-squares sense between the synthetic and filtered observed data generally below 10 Hz. The simplification to the full-space homogeneous model is valid when the receivers are deployed deep in the subsurface and close to the induced events, such as deploying borehole monitoring sensors in the vicinity of the hydraulic well, or when complexities in rock structure are not large compared to the frequencies recorded.

To retrieve reliable solutions, we developed a method to use high-frequency, full waveform information (both P and S) to determine the focal mechanisms of small earthquakes (Li et al., 2011). Using the known velocity model (one-dimensional layered model in this study), we calculate the Green's functions for all moment tensor components of the source at each location (hypocenter) and then the synthetic seismograms by convolving them with the source time function. To find the best match between the observed and synthetic seismograms, we formulate an objective function that incorporates information from different attributes in the waveforms: the cross-correlation values between the modeled waveforms and the data, the L_2 norms of the waveform differences, and the polarities of the first P arrivals and the S/P average amplitude ratios. Compared to previous studies, our method uses more attributes of seismograms to better determine the focal mechanisms of induced seismicity. The "high frequency" referred to in our study (several hertz for the shallow network and tens of hertz for the deep network) is a relative term: it is much higher than the frequency band (0.05–0.5 Hz) often used in the study of large earthquakes (e.g., Tan and Helmberger, 2007), but it is lower than the frequency band often used for exploration seismic imaging (e.g., Etgen et al., 2009). Essentially,

the frequency bands used in our study include a considerable portion of the energy radiated from the source; thus, the waveforms have good signal-to-noise ratio (S/N) and can reflect the characterizations of the source rupture.

Compared with full waveform tomography or migration techniques, which focus on improving the knowledge of the subsurface structures illuminated by simple active sources with known signatures (e.g., explosion or vibration source with known location and origin time; similar frequency, amplitude, radiation pattern, etc., are expected for all shots), the source mechanism determination method assumes the velocity model input, and focuses on determining the complicated source signature associated with the events. For induced seismicity in oil and gas fields, the velocity model is generally known from seismics and well logs. Comprehensive synthetic tests with random velocity perturbations are also performed to examine the robustness of our algorithm in the presence of the velocity uncertainties.

Previously, we tested our newly developed focal mechanism determination method on induced microearthquakes monitored by a five-station surface network at an oil field in Oman (Li et al., 2011). The field, operated by Petroleum Development Oman (PDO), was discovered in 1962 and put into production in 1969. An official program to monitor induced seismicity using a surface station network in the field commenced in 1999, and a borehole network was installed in February of 2002. The primary objective of this passive seismicity monitoring program was to locate the events and to correlate them with production and injection activities to understand and monitor the cause of induced seismicity in the field. In this paper, we apply the newly developed focal mechanism determination method to data from the borehole network. The source mechanisms determined using the borehole network are compared to those determined using the surface network. The robustness of the method is tested extensively on synthetic data sets generated for both the surface and borehole networks using a randomly perturbed velocity model.

INDUCED MICROEARTHQUAKE DATA SET

The petroleum field discussed in this paper is a large anticline created by deep-seated salt movement (Sarkar, 2008). The dome is about 15×20 km in size with a northeast-southwest axial elongation that is probably a result of regional deformation. The structure is dominated by a major central graben and two systems of faulting with two preferred directions (southeast-northwest and northeast-southwest) that affect the trapping mechanism in the oil reservoir. The northeast-southwest major network of faults and fractures partially connects all parts of the fields (Figures 1, 2). The main oil production is from the Lower Cretaceous Shuaiba chalk overlain unconformably by Nahr Umr shale, while gas is produced from the shallower Natih Formation overlain by the Fiqh shale Formation (Sarkar, 2008; Zhang et al., 2009).

Since 1996, increasing seismic activity has been reported by the staff working in the field. Significant surface subsidence in the center of the field has also been observed by InSAR, GPS, and leveling surveys, and has been attributed to compaction of the Natih formation (Bourne et al., 2006). To monitor the induced seismicity in the field, PDO first deployed a surface array of monitoring stations in 1999 (Figure 1). The stations are instrumented with SM-6B geophones with a natural frequency (f_n) of 4.5 Hz. In 2002, another network, independent of the shallow network, was installed in

the field as part of a Shell/PDO collaborative study (Figure 2). Unlike the surface array/shallow network, this network had borehole installations of seismic sensors (SM-7m, $f_n = 30$ Hz) at multiple levels, roughly ranging from depths of 750 to 1250 m. The instrumentation for this network was much deeper than that of the surface network, and therefore, this monitoring network is referred to as the “borehole network.” A schematic diagram of the wells and sensor positions is shown in Figure 2. The borehole network consisted of five closely spaced monitoring wells in the most seismically active part of the reservoir and covered a much smaller area than the surface network. Due to sensor positions at depths, the ability to acquire data at much higher frequencies and the proximity to the two producing units (Natih gas and Shuaiba oil), the deep network recorded much smaller magnitude events than the shallow network, resulting in a greatly increased detectability of induced seismicity (roughly about 25 times more induced events per day) compared to the shallow network. The borehole network was operational for about 18 months starting in February 2002; however, only microseismic data from the last 11 months (October 2002–August 2003) were available for this study. During that 11-month monitoring per-

iod, about 15,800 events were identified with an average rate of ~ 47 /day, out of which we analyzed and located about 5,400 events (Sarkar, 2008). Attempts were made to select common events detected during this period by both (deep and shallow) networks for a joint location analysis; however, due to clock synchronization problems and difference in sensor frequency bands between the two networks, the common events could not be identified, and hence the task could not be accomplished. Some research indicated that by carefully identifying the largest events in different networks, synchronization between networks sometimes can be achieved by shifting the origin times in one network with a constant time (Eisner et al., 2010). A similar strategy will be adopted in the future.

During the period of 1999 to 2007, over 1500 induced earthquakes were recorded by the surface network, and their occurrence frequency was found to be correlated with the amount of gas production (Sarkar, 2008). The distribution of induced events in the field recorded by the surface network is shown in Figure 1 (Sarkar, 2008; Sarkar et al., 2008; Zhang et al., 2009). All the events have a residual traveltimes of less than 30 ms, indicating they are well located. Figure 2 shows the microearthquake locations determined using the deep borehole network and the double-difference tomography method (Zhang et al., 2009). The root-mean-square

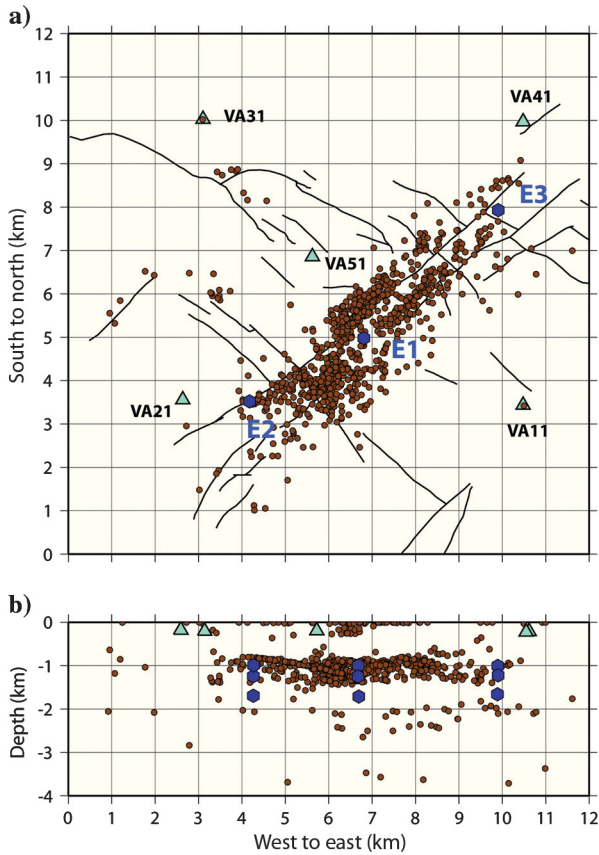


Figure 1. Distributions of near-surface stations and located events. (a) Map view of the studied field. The blue hexagons (E1, E2, and E3) are the epicenters of synthetic events and the green triangles (VA11, VA21, VA31, VA41, and VA51) are the five near-surface stations. These stations are located in shallow boreholes, 150 m below the surface, to increase the signal-to-noise ratio (S/N). The black lines are the identified faults. (b) Side view of the studied field. Most of the induced microearthquakes are localized around 1 km below the surface. A few shallow events have the largest traveltimes among all events.

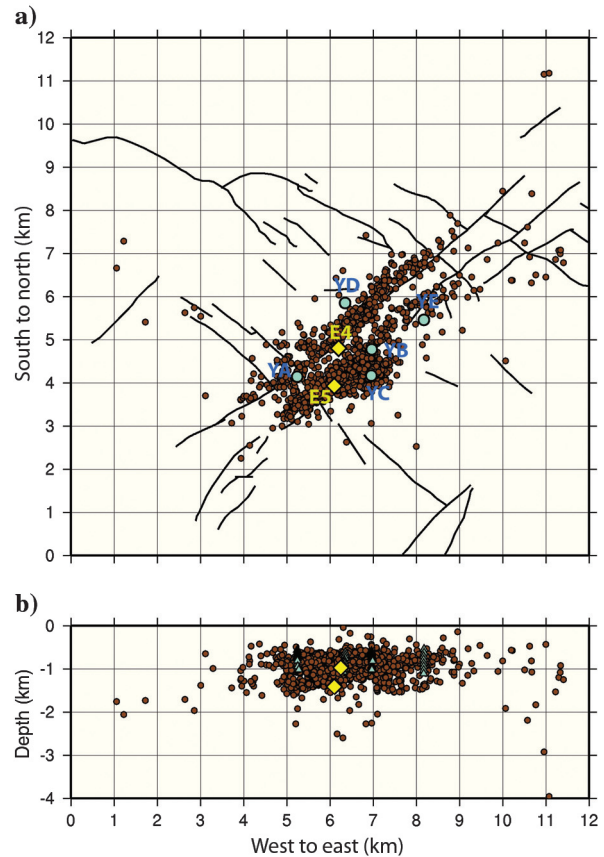


Figure 2. (a) Map view of the borehole network and the microearthquakes located by this network. The yellow diamonds (E4, E5) are the epicenters of synthetic events. The green circles are the surface locations of the five wellbores where receivers are installed. (b) Side view of the borehole network and located microearthquakes. The green triangles indicate the borehole stations. The vertical distance between two consecutive receivers in a monitoring well ranges from ~ 20 to ~ 70 m.

traveltime residual is around 10 ms (Zhang et al., 2009). In the map view, the earthquakes can be found mainly distributed along the mapped two northeast-southwest fault systems. This earthquake distribution suggests that most of the earthquakes are induced by the reactivation of the existing faults in the field. Figure 3 and Figure 4 show typical events and their spectrograms recorded by the surface network and borehole network, respectively. Because of the proximity of the earthquake source to the deep borehole network, the frequency content of the recorded waveform by the borehole network is much higher than by the surface network. For the waveforms recorded by the surface network, there is a considerable amount of energy in the frequency range of 3 to 9 Hz (Figure 3). For the deep borehole network, the recorded waveforms contain significant energy between 15 to 35 Hz (Figure 4).

FOCAL MECHANISM DETERMINATION METHOD

A detailed description of the method can be found in Li et al. (2011). Here, the method is briefly explained. The focal mechanism can be represented by a three-by-three second order moment tensor with six independent components (Aki and Richards, 2002). Here, we assume the focal mechanism of the small induced events can be represented by pure double couples (Rutledge and Phillips, 2002), though it is possible that a volume change or compensated linear vector dipoles (CLVD) part may also exist, especially in hydraulic fracturing cases, and the non-double-couple components are informative for understanding the rock failure under high-pressure fluid (Ross and Foulger, 1996; Jechumtálová and Eisner, 2008; Šílený et al., 2009; Song and Toksoz, 2010). The constraining of focal

Figure 3. The vertical components of seismograms of a typical event recorded by the surface network and the corresponding spectrograms. The filtered seismograms (3 ~ 9 Hz) are in the left column; the original seismograms are in the middle; the spectrograms of the original seismograms are at the right. The zero time is the origin time of the event.

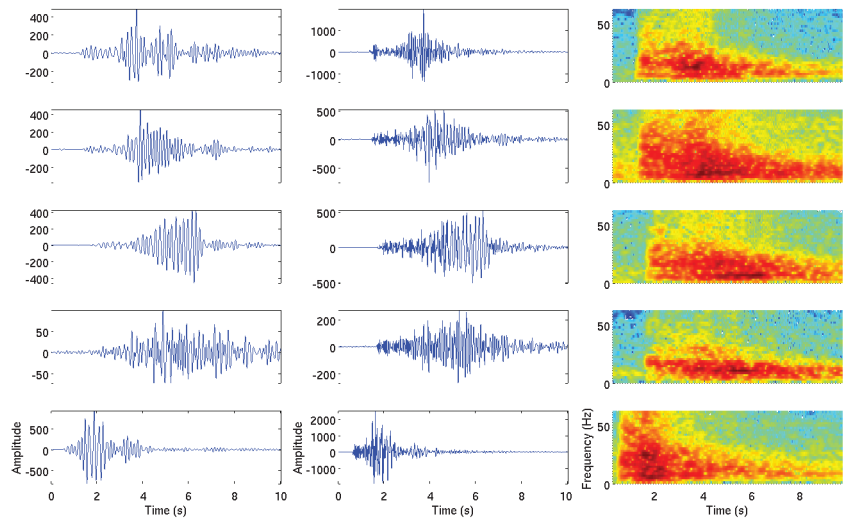
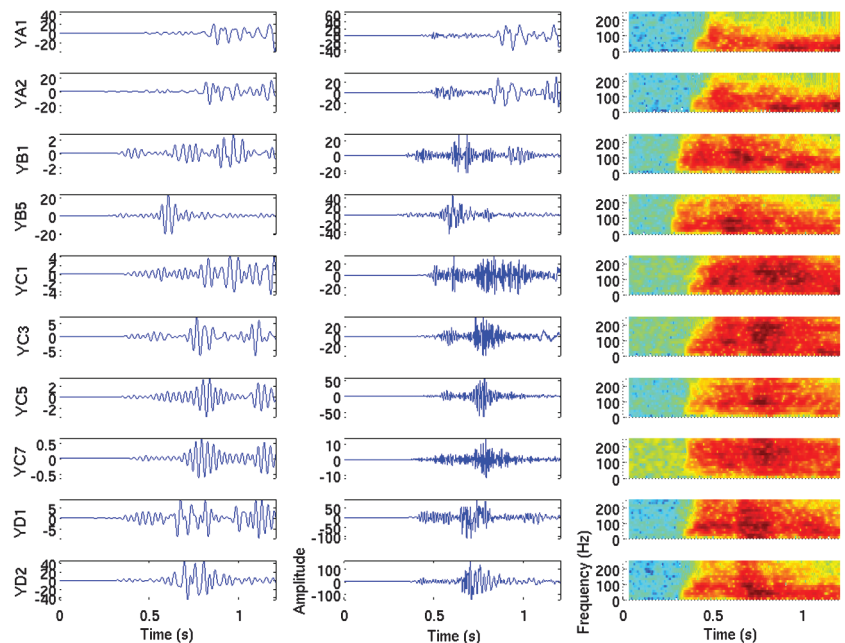


Figure 4. The vertical components of seismograms of a typical event recorded by the borehole network. The filtered seismograms (15 ~ 35 Hz) are in the left column; the original seismograms are in the middle; the spectrograms of the original seismograms are at the right. The zero time is the origin time of the event. It should be noted that the borehole data are dispersive, i.e., higher frequency contents arrive later as the energy is trapped within layers and propagates as guided waves.



mechanism as double couple (DC) can eliminate the spurious non-DC components in the inversion raised by modeling the wave propagation in anisotropic medium with isotropic Green's functions or inaccuracy of the velocity model (Šílený and Vavryčuk, 2002; Godano et al., 2011). However, if strong non-DC components actually exist in the source rupture process, the determined fault plane may be biased (e.g., Jechumtálová and Šílený, 2001, 2005). In our analysis, we describe the DC focal mechanism of seismic source in terms of its strike (Φ), dip (δ), and rake (λ), and determine double couple components from these three parameters. The simplification of the source is supported by the observation that almost all the detected microearthquakes occurred along preexisting faults, i.e., reactivated faults slipping along preexisting weak zones would not cause significant volumetric or CLVD components (Julian et al., 1998). For each component of a moment tensor, we use the discrete wavenumber method (DWN) (Bouchon, 1981, 2003) to calculate its Green's functions $G_{ij,k}^n(t)$ for the horizontally layered medium. Appendix A gives the modified reflectivity matrix for computing the seismograms when the receiver is deeper than the source, such as in the borehole monitoring case. It should be noted that if the full moment tensor needs to be determined, e.g., in the hydraulic fracturing cases, the seismic source should be described with six independent tensor components, which will increase the cost in searching for the best solution. The structure between the earthquake and the station is represented as a 1D horizontally layered medium, which can be built from (1) averaging borehole sonic logs across this region, or (2) extracting the velocity structure between the source and the receiver from the 3D velocity model from double-difference seismic tomography for passive seismic events (Zhang et al., 2009).

The modeled waveform from a certain combination of strike, dip, and rake is expressed as a linear combination of weighted Green's functions:

$$V_i^n = \sum_{j=1}^3 \sum_{k=1}^3 m_{jk} G_{ij,k}^n(t) * s(t), \quad (1)$$

where V_i^n is the modeled i th (north, east, or vertical) component at station n ; m_{jk} is the moment tensor component and is determined by the data from all stations; $G_{ij,k}^n(t)$ is the i th component of the Green's functions for the (j, k) entry at station n , and $s(t)$ is the source time function. In this study, a smooth ramp is used for $s(t)$, the duration of which can be estimated from the spectra of the recorded seismograms (Bouchon, 1981). The source time functions are found to be insensitive to the waveform fitting, as both the synthetic and observed seismograms are low-pass filtered before comparisons (Zhao et al., 2006). Using reciprocity by straining Green's tensors can improve the efficiency of calculating the Green's functions, especially when the sources greatly outnumber the stations (Eisner and Clayton, 2001; Zhao et al., 2006). For instance, only one numerical simulation with reciprocity (e.g., finite difference method), by setting a source at a station, is needed to calculate the Green's functions for all six components of the moment tensor between anywhere in the field and one component at the station in a 3D heterogeneous medium.

Earthquake locations are usually provided by the traveltimes location method. However, due to uncertainties in velocity model and arrival times, the seismic event locations may have errors, especially in focal depth determined from the surface network. While

matching the modeled and observed waveforms, we also search for an improved location (x, y, z) around the catalog location.

To determine the best solution, we construct an objective function that characterizes the similarity between the modeled and observed waveforms. We use the following objective function, which evaluates four different aspects of the waveform information:

$$\begin{aligned} \text{maximize}(J(x, y, z, \Phi, \delta, \lambda, t_s)) = & \\ & \sum_{n=1}^N \sum_{j=1}^3 \left\{ \alpha_1 \max(\tilde{d}_j^n \otimes \tilde{v}_j^n) - \alpha_2 \|\tilde{d}_j^n - \tilde{v}_j^n\|_2 \right. \\ & \left. + \alpha_3 f(\text{pol}(\tilde{d}_j^n), \text{pol}(\tilde{v}_j^n)) + \alpha_4 h \left(\text{rat} \left(\frac{S(d_j^n)}{P(d_j^n)} \right), \text{rat} \left(\frac{S(v_j^n)}{P(v_j^n)} \right) \right) \right\}. \end{aligned} \quad (2)$$

Here \tilde{d}_j^n is the normalized data and \tilde{v}_j^n is the normalized modeled waveform; x, y , and z are the event hypocenter that will be redetermined by waveform matching; t_s is the time shift that gives the largest crosscorrelation value between the observed and synthetic seismograms (first term). Because it is difficult to obtain accurate absolute amplitudes due to site effects in many situations, we normalize the filtered, observed, and modeled waveforms before comparison. The normalization used here is the energy normalization, such that the energy of the normalized wavetrain within a time window adds to unity. Compared to peak amplitude normalization, energy normalization is less affected by site effects, which may cause abnormally large peaks due to focusing and other factors. In a concise form, this normalization can be written as

$$\tilde{d}_j^n = \frac{d_j^n}{\sqrt{\int_{t_1}^{t_2} (d_j^n)^2 dt}} \quad (3)$$

where t_1 and t_2 are the boundaries of the time window.

The objective function J in equation 2 consists of four terms. α_1 through α_4 are the weights for each term. Each weight is a positive scalar number and is optimally chosen in a way such that no single term will overdominate the objective function. We used $\alpha_1 = 3$, $\alpha_2 = 3$, $\alpha_3 = 1$ and $\alpha_4 = 0.5$ for the synthetic tests and real events. The first term in equation 2 evaluates the maximum crosscorrelation between the normalized data (\tilde{d}_j^n) and the normalized modeled waveforms (\tilde{v}_j^n). From the crosscorrelation, we find the time-shift (t_s) to align the modeled waveform with the observed waveform. The second term evaluates the L_2 norm of the direct differences between the aligned modeled and observed waveforms (note the minus sign of the second term to minimize the amplitude differences). The first two terms are not independent of each other, however, they have different sensitivities at different frequency bands and by combining them together the waveform similarity can be better characterized. The third term evaluates whether the polarities of the first P-wave arrivals as observed in the data are consistent with those in the modeled waveforms. The pol is a weighted sign function which can be $\{\beta, -\beta, 0\}$, where β is a weight reflecting our confidence in picking the polarities of the first P-wave arrivals in the observed data. Zero (0) means undetermined polarity; f is a function that penalizes the polarity sign inconsistency in such a way that the polarity consistency gives a positive value, while polarity inconsistency gives a negative value. The matching of the first P-wave polarities between

modeled and observed waveforms is an important condition for determining the focal mechanism, when the polarities can be clearly identified. Polarity consistency at some stations can be violated if the polarity is not confidently identified (small β) and the other three terms favor a certain focal mechanism. Therefore, the polarity information is integrated into our objective function in a flexible way. By summing over the waveforms in a narrow window around the arrival time and checking the sign of the summation, we determine the polarities robustly for the modeled data. For the observed data, we determine the P-wave polarities manually.

The fourth term in the objective function is to evaluate the consistency of the average S/P amplitude ratios in the observed and modeled waveforms (Hardebeck & Shearer, 2003). The ‘‘rat’’ is the ratio evaluation function and it can be written as

$$\text{rat} = \frac{\int_{T_2}^{T_3} |r_j^n(t)| dt}{\int_{T_1}^{T_2} |r_j^n(t)| dt}, \quad (4)$$

where $[T_1 T_2]$ and $[T_2 T_3]$ define the time window of P- and S-waves, respectively, and r_j^n denotes either d_j^n or v_j^n . The term h is a function that penalizes the ratio differences so that the better matching gives a higher value. Note that here we use the unnormalized waveforms d_j^n and v_j^n .

In general, the amplitudes of P-waves are much smaller than those of S-waves. To balance the contribution between P- and S-waves, we need to fit P- and S-waves separately using the first two terms in equation 2. Also, by separating S- from P-waves and allowing an independent time-shift in comparing observed data with modeled waveforms, it is helpful to deal with incorrect phase arrival time due to incorrect V_P/V_S ratios (Zhu and Helmberger, 1996). Here, we allow independent shifts for different stations as well as for P- and S-waves. We calculate both the first P- and S-arrival times by the finite difference eikonal solver (Podvin and Lecomte, 1991). The wavetrain is then separated into two parts at the beginning of the S-wave. The window for the P-wave comparison is from the first arrival to the beginning of the S-wave, and the window for the S-wave comparison is proportional to the epicenter distance. It should be noted that the full wavetrain is not included as later arrivals, usually due to scattering from heterogeneous media, cause larger inaccuracies in waveform modeling.

In some cases, when we have more confidence in some stations, e.g., stations with short epicenter distance, or stations deployed on known simpler velocity structure, we can give more weight to those stations by multiplying α_1 - α_4 with an additional station weight factor.

The comparison algorithm (equation 2) is optimized such that it can be performed on a multicore desktop machine usually within 30 minutes, even when tens of millions of synthetic traces are compared with the data. The computation of the Green’s function library using DWN takes more time, but it only needs to be computed once.

The passive seismic tomography only provides a detailed 3D velocity model close to the central area of the field due to the earthquake-station geometry (Zhang et al., 2009). Therefore, for the focal mechanism determination through the surface network, of which most stations are not placed within the central area (Figure 1), we use the 1D layered velocity model from the averaged sonic logs (Sarkar, 2008; Zhang et al., 2009). Considering that we use a frequency band of 3–9 Hz (Figure 3) in our waveform matching for this surface network, corresponding to a dominant P-wave

wavelength of 800 m and S-wave wavelength of 400 m, the velocity model should satisfy our modeling requirement. The deep network consists of five boreholes with eight levels of receivers at different depths in each borehole (Figure 2). Due to the proximity of borehole receivers to the seismicity, we were able to record the seismograms of very small induced seismicity. Waveforms between 15 and 35 Hz are used to determine the focal mechanisms (Figure 4). To better model the waveforms, we replaced part of the 1D average layered velocity model with the extracted P- and S-wave velocities from the 3D tomographic model between 0.7 km and 1.2 km in depth, where it has the highest resolution and reliability. Note that the updated 1D velocity model between the earthquake and each station becomes different for the deep borehole network.

SYNTHETIC TESTS FOR THE SURFACE AND DEEP BOREHOLE NETWORKS

In Li et al. (2011), we tested the robustness of the method on the surface network. To account for the uncertainty of the 1D velocity model, a 5% random perturbation was applied. Here, we consider a greater uncertainty in the velocity model — up to 8% — and test more cases for different focal mechanisms and event locations. We first use the station configuration of the surface network in our test because it provides a considerable challenge due to the large epicenter distance and the relative inaccuracy in the computation of Green’s functions by using the 1D averaged velocity model from several sonic logs. We choose three different epicenters (E1, E2, and E3), and for each epicenter we choose three different depths (D1 = 1000 m, D2 = 1200 m, and D3 = 1700 m), corresponding to shallow, medium, and deep events in this field, respectively. At each depth, we test three different focal mechanisms, which yield 27 different synthetic tests in total. The different focal mechanisms and widely distributed hypocenters in the synthetic test give a comprehensive robustness test for the focal mechanism determination in this region. The station configuration and the hypocenter distribution are shown in Figure 1. At each hypocenter, three distinct mechanisms are tested, namely M1: $\Phi = 210^\circ$, $\delta = 50^\circ$, $\lambda = -40^\circ$; M2: $\Phi = 50^\circ$, $\delta = 60^\circ$, $\lambda = -70^\circ$; and M3: $\Phi = 130^\circ$, $\delta = 80^\circ$, $\lambda = 80^\circ$ (Table 1). Three or four first P-arrival polarities are used in each synthetic test, resembling the measurements we have for real data for this surface network. In real cases, as inevitable differences exist between the derived velocity model and the true velocity model, we need to examine the robustness of our method under such circumstances. We add up to 8% of the layer’s velocity as the random velocity perturbation to the reference velocity model in each layer (Figure 5) and use the perturbed velocity models to generate synthetic data. The perturbation is independent for five stations, i.e., the velocity model is path-dependent and varies among different event-station pairs to reflect the 3D velocity heterogeneities in the field. Also, the perturbation is independent for the P-wave and S-wave velocities in a specific velocity model for an event-station pair. The Green’s functions (modeled data) are generated with the reference velocity model. Figure 6 shows the modeled seismograms with offset using the reference velocity model. The predicted traveltimes by the eikonal equation and the first arrivals in the waveforms are matched well. It should also be noted that the P-wave and S-wave velocity perturbation from one station to another can reach up to 800 m/s in some layers. Considering that this reservoir consists mainly of sedimentary rocks, the magnitude of the random lateral velocity perturbation should reflect the upper bounds of the local

lateral velocity inhomogeneity. The density is not perturbed in this test, as the velocity perturbation is dominant in determining the characteristics of the waveforms. The test results are summarized in Table 1. Although the perturbation can change the waveform characteristics to a very large extent, the synthetic test shows that our method can still find a solution very close to the correct one by including information from different aspects of the waveforms, even when only records from five vertical components are used. Figure 7 shows a waveform match between the synthetic data and the modeled data. The best solution found is (230°, 60°, -40°), close to the correct solution (210°, 50°, -40°) in comparison. The synthetic event is at 1220 m in depth.

In general, the focal mechanisms are reliably recovered (Table 1). To quantify the recoverability, we define the mean recovery error for the focal parameters:

$$\Delta\varphi_m^e = \frac{\sum_{d=1}^3 |\varphi_{m,d}^e - \varphi_m|}{3}, \quad (7)$$

where $\varphi_{m,d}^e$ is the recovered strike, dip, or rake for epicenter e , with mechanism m at depth d , where $e, m, d \in \{1, 2, 3\}$, and φ_m is the reference (true) focal parameter for mechanism m . It is found that $\Delta\varphi$ is only a weak function of epicenter, with marginally smaller

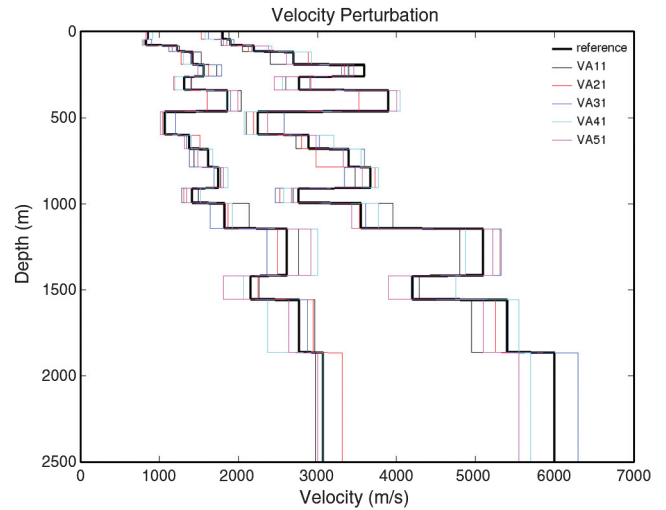


Figure 5. P- (right) and S-wave (left) velocity perturbations for the synthetic tests. The reference velocities, plotted with the bold black line, are used for calculating the Green's functions. The perturbed velocities (colored lines) are used to generate the synthetic data for each station.

Table 1. Recovered focal mechanisms in the synthetic tests for different hypocenters and faulting types. The true focal mechanisms are listed in the row indicated by REF. Rows D1, D2, and D3 list the events at 1000 m, 1200 m, and 1700 m in depth, respectively.

	E1			E2			E3		
	M1	M2	M3	M1	M2	M3	M1	M2	M3
REF									
D1									
D2									
D3									
$\Delta\Phi^\circ$	16	23	6	10	20	26	6	14	20
$\Delta\delta^\circ$	20	3	3	13	6	6	6	10	3
$\Delta\lambda^\circ$	3	10	13	3	27	10	16	8	18

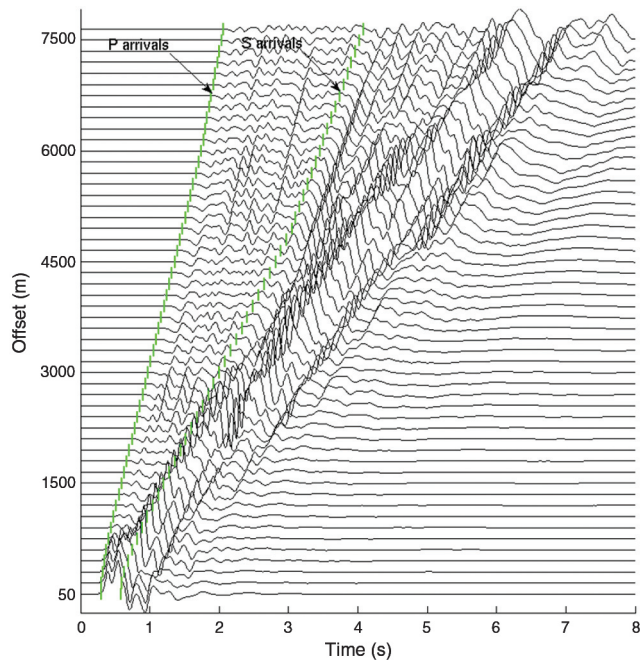
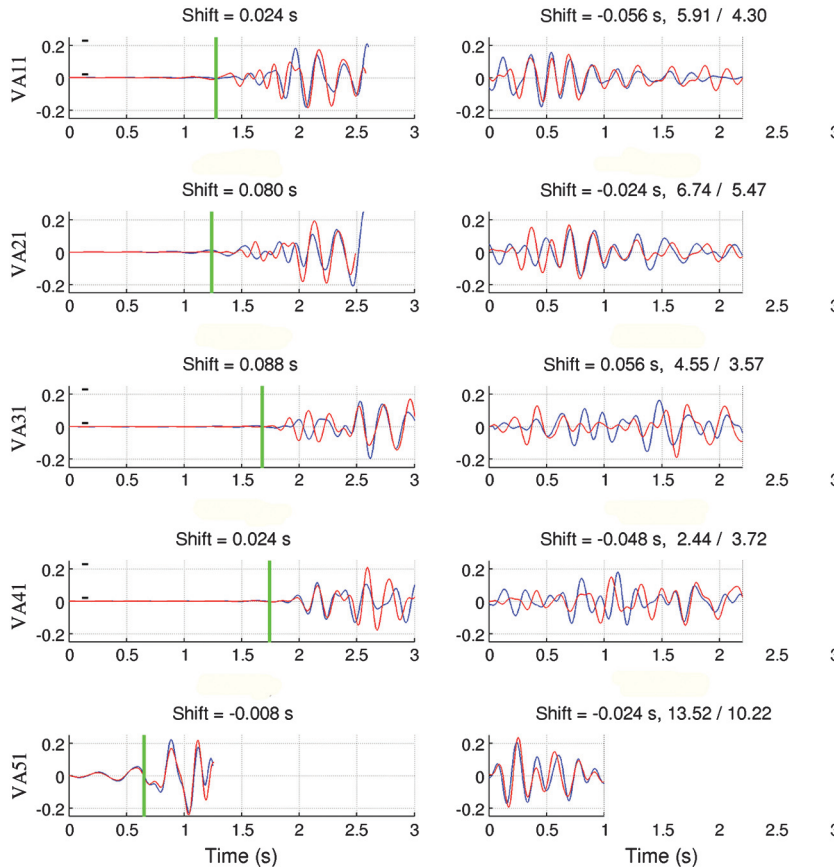


Figure 6. Moveouts of the P- and S-waves with distance. The source is at 900-m depth, and the receivers (vertical components) are at 150-m depth. The green lines indicate the first P- and S-wave arrivals obtained from finite-difference traveltimes calculation method based on the eikonal equation.

Figure 7. Comparisons between modeled waveforms (red) and synthetic data (blue) at five stations with perturbed velocity model. From top to bottom, waveforms from the vertical components at stations one through five, respectively, are shown. The waveforms are filtered between 3 and 9 Hz. The left column shows P-waves and right column shows S-waves. The green lines indicate the first P-arrival times. For P-waves, zero time means the origin time, and for S-waves, zero time means the S-wave arrival time predicted by the calculated traveltimes. The “shift” in the title of each subplot indicates the time shifted in the data to align with the synthetic waveforms. In the left column, the + or - signs indicate the first-arrival polarities of P-waves in the synthetic data and those in the modeled data, respectively. In the right column, the number to the left of the slash denotes the S/P amplitude ratio for the synthetic data, and the number to the right of the slash denotes the ratio for the modeled waveform.



value for E1 than for E2 or E3, in general. Also, we found that for each individual depth $\Delta\phi$ ($d = 1, 2, \text{ or } 3$) is marginally smaller for shallower earthquakes (D1 and D2) than for deeper earthquakes (D3) (results not tabulated). Due to our use of only vertical components, we found that the uncertainty in strike is slightly larger than that in dip or rake. In general, no distinct variation of $\Delta\phi$ is found against the hypocenter or faulting type. Therefore, we conclude that our method is not very sensitive to the faulting type, to the azimuthal coverage of the stations, or to the hypocenter position within a reasonable range for the array geometries studied.

For the borehole network, we perform a similar synthetic test to check the reliability of our method for the deep network configuration. As we have shown that the reliability of our method is not very sensitive to the azimuthal coverage of the stations or to the depth of the event in a reasonable range, we only perform synthetic experiments at two hypocenters with three different mechanisms, respectively, for the deep borehole network (Table 2). Nine to eleven receivers are used for each case. The frequency band is the same as we used for the real data set (15–35 Hz). A typical waveform comparison for the synthetic test is shown in Figure 8. It is also found that the method is robust with the borehole receiver configuration using higher frequency seismograms.

APPLICATION TO FIELD DATA

We applied this method to study 40 microearthquakes using surface and deep borehole networks. The instrumental responses have been removed before processing. An attenuation model with Q value increasing with depth (Table 3) was used for the waveform

modeling. In general, we consider the attenuation larger (smaller Q) close to the surface due to weathering, and the attenuation for S-waves larger than for P-waves at the same depth. The attenuation model is built from empirical knowledge of the local geology, and we also tested that reasonable deviation from our Q model (50%) causes only small changes in our synthetic waveforms. Figure 9 shows the beachballs of the nine best solutions out of millions of trials for a typical event recorded by the surface network. Our best solution (the one at the bottom right, reverse strike-slip) has a strike of 325° , which is quite close to the best known orientation 320° of the northwest-southeast conjugate fault (Figure 1). Figure 10 shows the comparison between the modeled and the observed data for this event. The waveform similarity between the modeled and observed data is good. Typically, the crosscorrelation coefficient is greater than 0.7. Additionally, the S/P waveform amplitude ratios in the modeled and observed data are quite close, and the first P arrival polarities are identical in the modeled and observed data for each station. In this example, all four criteria in equation 2 are evaluated, and they are consistent between the modeled and observed data.

For the deep borehole network, we use the frequency band 15 ~ 35 Hz, which includes enough energy in the spectra to provide good S/N, for determining the focal mechanisms of these small magnitude earthquakes from the borehole network data (Figure 4). The lower frequency here is limited by the bandwidth of the borehole instrumentation ($f_c = 20$ Hz), and the frequency contents below the corner frequency f_c may suffer from an increased noise level. As there is also uncertainty in the orientations of the horizontal components, we use only the vertical components of the 4C sensors configured in a proprietary tetrahedral shape for each level (Jones et al., 2004). Although there are, in total 40, vertical receivers, we often only use about 10 seismograms in determining each event due to the following reasons:

- Some receivers are only separated by ~30 m vertically and therefore do not provide much additional information for determining the source mechanism.
- Some traces show peculiar, unexplainable characteristics in seismograms and are, therefore, discarded. The S/N for some traces is also very poor.

In our selection of seismograms, we try to include data from different wells to provide a better azimuthal coverage, as well as from different depths spanning a large vertical range, providing waveform samplings at various radiation directions of the source.

Figure 11 shows the comparison between the observed and modeled seismograms for a typical event recorded by the deep borehole network. Eleven receivers from four boreholes are used in this determination. Among the eleven seismograms, five first P-wave arrival polarities are identified and then used in this determination. The waveform similarities, average S/P amplitude ratio, and consistency in the P-wave arrival polarities are satisfactory. Comparing Figure 11 with Figure 10, we found the fewer matched cycles in the deep borehole case. Similar comparison can also be found between the shallow and deep borehole synthetic tests (Figures 7 and 8),

where focal mechanisms close to the correct solutions were still found in both synthetic cases.

Using this method, we have studied 40 earthquakes distributed across this oil field from both the surface network and the borehole network. Among these studied events, 22 events are recorded by the surface network, 18 events are from the borehole network. Figure 12 shows that most of the events primarily have the normal faulting mechanism, some have the strike-slip mechanism, and some have a reverse faulting mechanism. The strike directions of most events are found to be approximately parallel with the northeast trending fault, suggesting the correlation of these events with the northeast trending fault. However, some events also have their strikes in the direction of the conjugate northwest trending fault, suggesting that the reactivation also occurred on the conjugate faults. Although the number of studied events is small compared to the total recorded events, their mechanisms still provide us with some insights on the fault reactivation in this field: (1) The hypocenter distribution and the determined source mechanisms (e.g., strikes) indicate that the reactivation of preexisting faults is the main cause of the induced microearthquakes in this field, and both the northeast trending fault and its conjugate fault trending in the northwest direction are still active. Interestingly, we note that the strike directions of the normal faulting events (red) are slightly rotated counterclockwise with respect to the mapped fault traces from the 3D active seismic data and are consistent with the trend of the located earthquake locations (Figure 1). (2) The counterclockwise rotation may be due to the nonplanar geometry of the fault, i.e., the strike of the shallow part of the fault as delineated by the surface seismic survey does not need to be the same as the deeper part of the fault, where most induced seismicity is located. Most strike-slip events (cyan) are shallow, suggesting that the maximum horizontal stress (S_{Hmax}) is still larger than the vertical stress (S_V) at this depth range. However, deeper events (e.g., red, blue) mainly have a normal faulting mechanism, suggesting S_V exceeds S_{Hmax} when depth increases beyond ~1 km in this region. The dominance of normal faulting is consistent with the study by Zoback and Zinke (2002) on the Valhall and Ekofisk oil fields, where reservoir depletion induced normal

Table 2. Recovered focal mechanisms in the synthetic tests for different faulting types using the deep borehole network. The true focal mechanisms are listed in the row indicated by REF. The synthetic events at two different hypocenters are tested (Figure 2).

	E4 (D = 1 km)			E5 (D = 1.4 km)		
	M1	M2	M3	M1	M2	M3
REF						
Best sol.						
$\Delta\phi^\circ$	10	50	20	30	10	30
$\Delta\delta^\circ$	10	10	40	10	10	0
$\Delta\lambda^\circ$	10	10	0	30	10	30

faulting in and above the productive horizon. In this oil field, most induced earthquakes occurred above the oil layer, which is located around 1.5 km below the surface. (3) Assuming $S_{H_{max}}$ is parallel with the strike of normal faulting events, perpendicular to the strike of reverse events, and bisects the two fault planes of the strike-slip events (Zoback, 2007), most of the determined events then suggest a $S_{H_{max}}$ trending northeast or north-northeast, which is consistent with the well breakout measurement and local tectonic stress analysis in the region (Al-Anboori, 2005). The observations indicate that the regional preexisting horizontal stress and the vertical stress played an important role in the reactivation of these preexisting faults.

DISCUSSION

Although we only applied our method to a particular oil/gas field, the method is applicable to any microseismic monitoring case, especially to cases when the monitoring stations are sparse. We only used the vertical components in our study, but the waveform comparison can be easily expanded to include three components. Considering each component at a station contains different information in the radiation pattern (Aki and Richards, 2002), the incorporation of multicomponent observations should further reduce the solution uncertainty.

The attenuation needs to be taken into account in the synthetic waveform modeling. Not only is the amplitude changed, but frequency-dependent phase-shift also occurs as the phase velocity

becomes dependent on frequency due to the attenuation effect (Aki and Richards, 2002). It should be noted that the attenuation-induced phase-shift is in addition to any phase-shift related to the wave propagation, e.g., guided wave effect. In our waveform modeling, compared to the pure elastic case we have observed notable waveform change in the frequency band of observation when moderate attenuation is included. Attenuation tomography (e.g., Quan and Harris, 1997) should be considered to construct an attenuation model if receivers are not located in the vicinity of the microseismic events.

Our synthetic test indicates that when there are errors in the velocity model, the inverted mechanisms are affected and can deviate from the true ones. Therefore, it is difficult to tell whether the oscillation in the inverted strike, dip, and rake is true or if it is caused by our limited observations and errors in the velocity model.

In general, we find the inversion results are not sensitive to the weighting parameters that are within reasonable ranges. The rule of thumb is to choose a parameter set that balances the contribution from each term in the objective function. The weighting parameters used in our study may not be optimal in other fields and need to be determined for individual data sets.

Although tens of millions of synthetic seismograms are usually compared with observed seismograms in the global grid search, some manipulation in the crosscorrelation and filtering (Li et al., 2011) can be used to greatly reduce the time consumption.

Figure 8. Comparisons between modeled waveforms (red) and synthetic data (blue) at nine borehole stations with the perturbed velocity model. In this test, nine vertical components in borehole YA, YB, YC, and YD are used. The waveforms are filtered between 15 and 35 Hz. The true mechanism is $(210^\circ, 50^\circ, -40^\circ)$, and the best recovered one is $(240^\circ, 60^\circ, -10^\circ)$ in comparison.

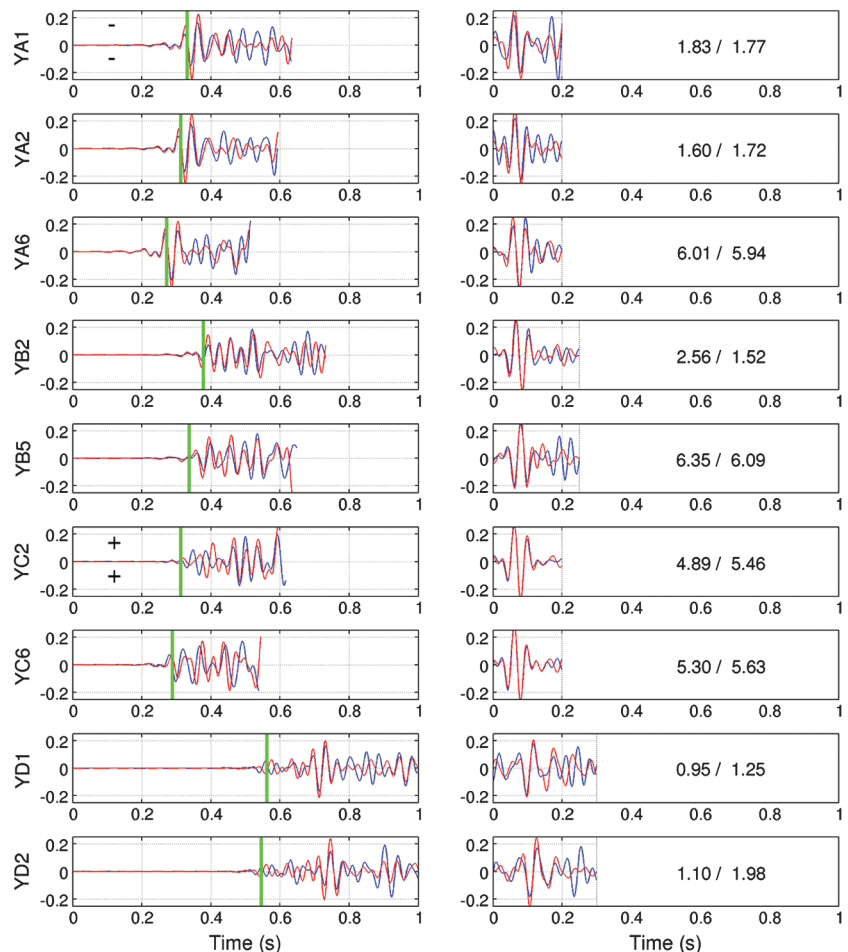


Table 3. One-dimensional attenuation model used for the DWN waveform modeling. The attenuation affects the waveform amplitudes and causes waveform dispersion.

Depth (m)	Q_P	Q_S
0–60	30	20
60–110	40	20
110–160	60	30
160–264	80	40
264–470	100	50
470–1090	200	100
1090–bot.	300	150

Additionally, our inversion algorithm can be easily parallelized. Our experience is that twenty million synthetic seismograms from different source mechanism and hypocenter combinations can be searched through on an eight-core workstation in about 20 minutes. Therefore, our algorithm can be easily extended to monitoring cases where many more stations and components are available.

Our methodology can also be applied to solve for the full moment tensor. In that case, we will have six independent moment tensor components m_{jk} associated with the source mechanism in our objective function. The increase in the degree of freedom will require more search time. In addition, it is more challenging to resolve the six independent moment tensor components because velocity model error, anisotropy or even the inconsistency in the source time function in different moment tensor components become the hindrance.

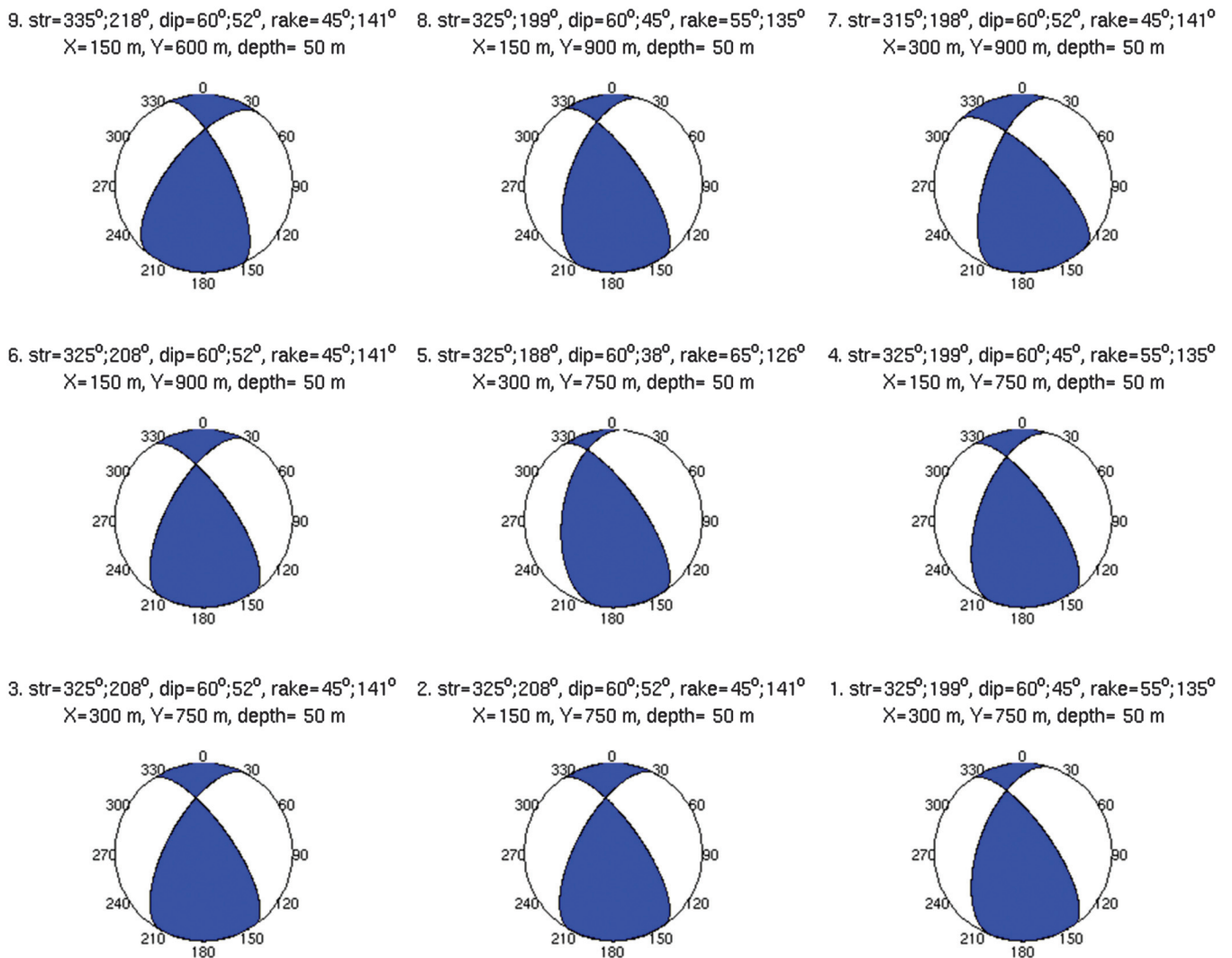


Figure 9. Focal mechanism solutions for a typical event determined by the shallow network. The one at the bottom right (#1) is the best solution with maximum objective function value. The epicenter is shifted northward (y) by about 750 m, eastward (x) by about 300 m and the depth is shifted 50 m deeper compared to the original hypocenter. The shift in epicenter may be biased by inaccuracy in the velocity model and by only using the vertical components. The shift can compensate the phase difference between the modeled seismograms and the real seismograms.

Figure 10. Comparison between the modeled waveforms (red) and the real data (blue) at five surface network stations for a typical event. For P-waves, zero time means the origin time, and for S-waves, zero time means the S-wave arrival time predicted by the calculated traveltimes.

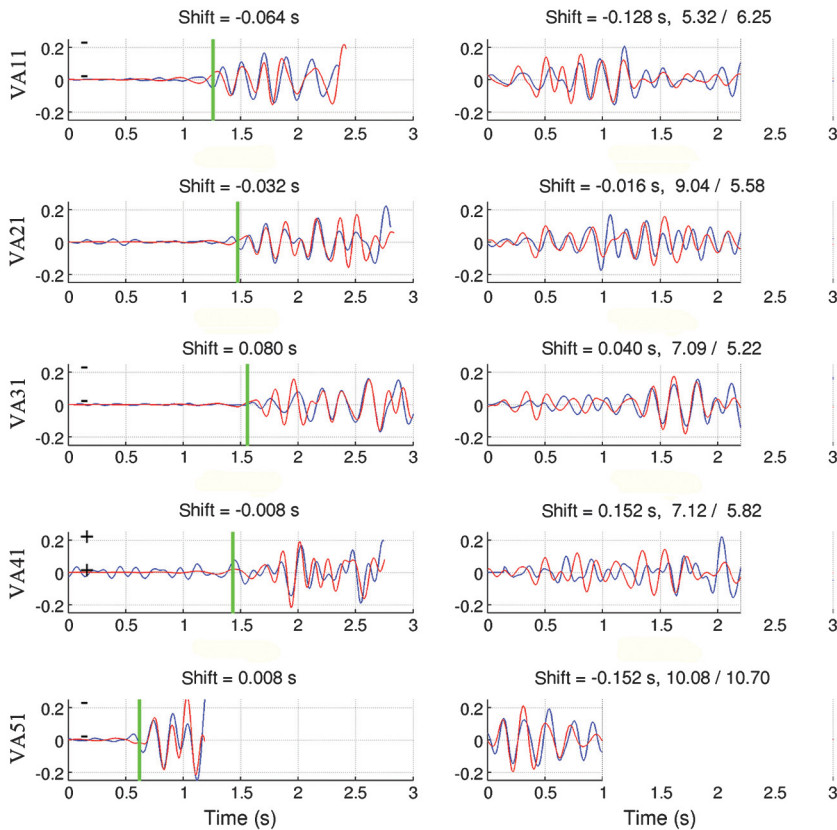
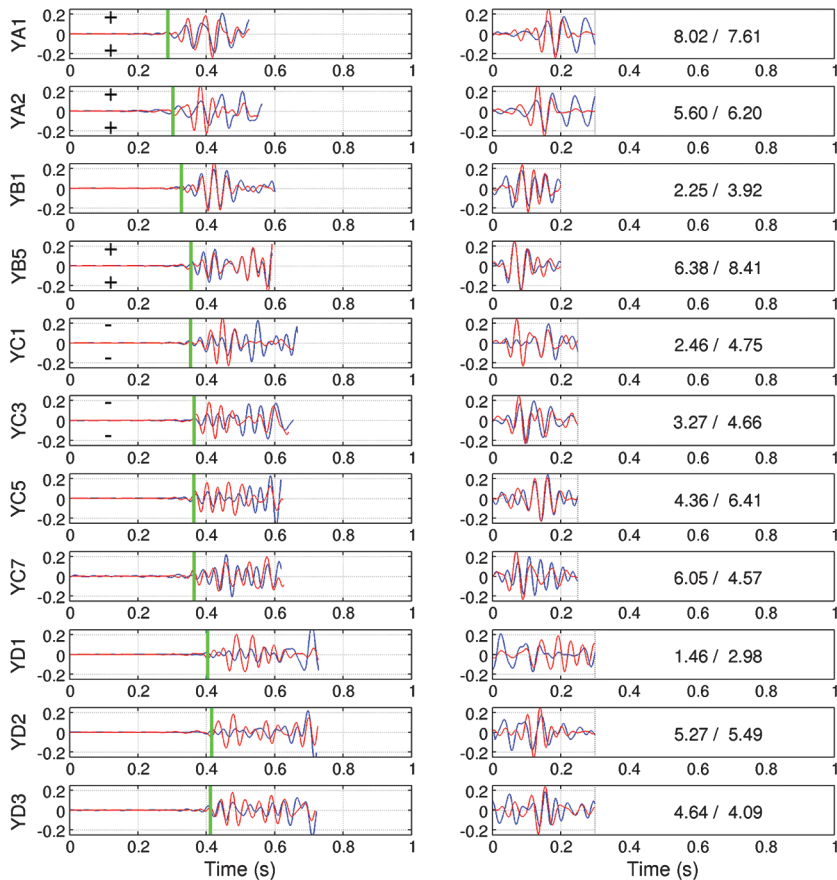


Figure 11. Comparison between the modeled waveforms (red) and the real data (blue) from the borehole network. Eleven stations and five first P-wave arrival polarities which can be clearly decided in the observed waveforms are used in this determination. For P-waves, zero time means the origin time, and for S-waves, zero time means the S-wave arrival time predicted by the calculated traveltimes.



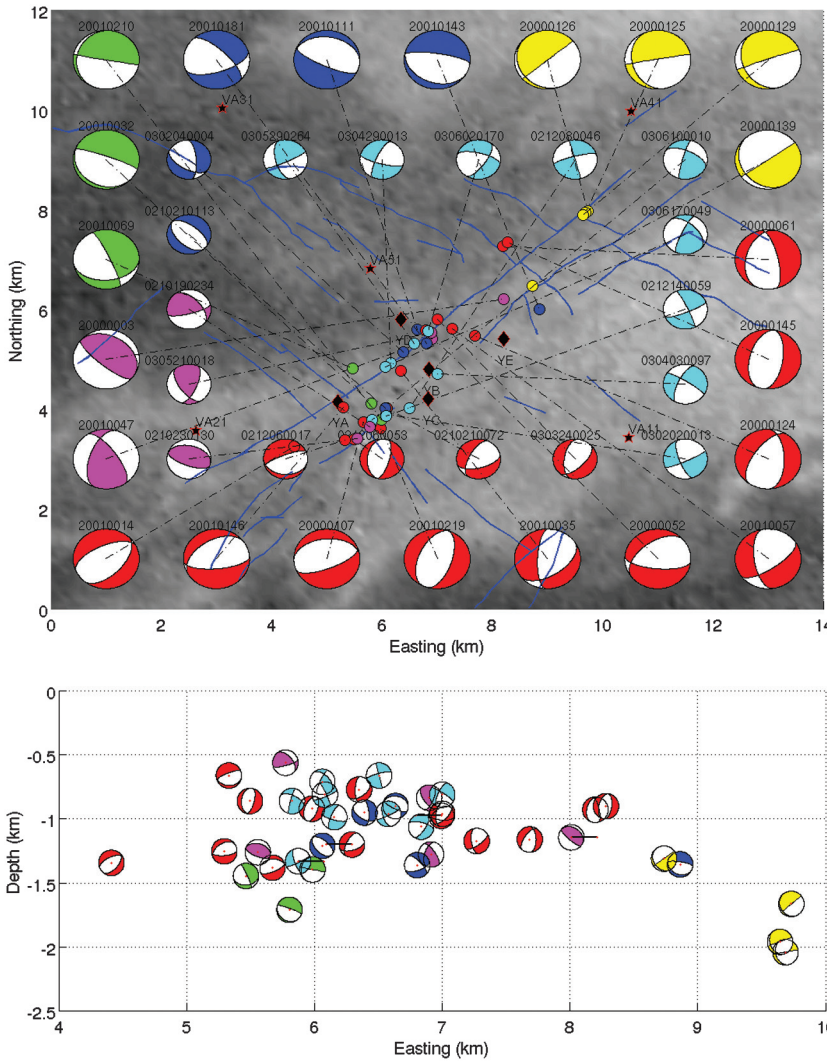


Figure 12. (a) Focal mechanisms of the 40 events inverted in this study from both the surface and borehole networks. The background color in the map indicates the local change in surface elevation with a maximum difference of about 10 m. Different focal mechanisms are grouped in several colors. The events and their focal mechanisms determined by the surface network are plotted in the outer perimeter, while the ones by the borehole network are plotted in the inner ring. (b) Side view of the depth distribution and focal mechanisms of the studied events. Because only vertical components are used in our focal mechanism determination, our results are not very sensitive to epicenter shifting. Therefore, the event epicenters shown in (a) are from the traveltime location and the event depths in (b) are from the waveform matching process.

CONCLUSIONS

In this study, we used our recently developed high-frequency waveform matching method to determine the microearthquakes in an oil field with the surface and borehole network data. This method is especially applicable to the study of microearthquakes recorded by a small number of stations, even when some first P arrival polarities are not identifiable due to noise contamination, or only the vertical components are usable. The objective function, formulated to include matching phase and amplitude information, first arrival P polarities and S/P amplitude ratios between the modeled and observed waveforms, yields reliable solutions. We also performed systematic synthetic tests to verify the stability of our method.

For the 40 studied events, we found that the hypocenters and strikes of the events are correlated with preexisting faults, indicating that the microearthquakes occur primarily by reactivation of the preexisting faults. We also found that the maximum horizontal stress derived from the source mechanisms trends in the northeast or north-northeast direction; this is consistent with the direction of the maximum horizontal stress obtained from well breakout measurements and local tectonic stress analysis. Our investigation shows

that the study of the source mechanisms of the induced microearthquakes can provide insights into the local stress heterogeneity and help to better understand the induced microearthquakes by oil or gas production.

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APPENDIX A

GREEN'S FUNCTIONS CALCULATION FOR THE DEEP BOREHOLE NETWORK

The reflectivity method used in the discrete wavenumber waveform modeling of Bouchon (2003) was originally developed in global seismology where sources are located underground and

receivers are at the surface or near the surface. For the surveys using borehole receivers, however, the receivers can be located deeper than the source; thus the original reflectivity method needs to be revised and calculations in the reflectivity method need to be modified for this configuration. We followed the symbols and definitions used in the paper by Muller (1985) on the reflectivity method and only show the key modified equations. Figure A-1 shows the diagram for borehole receiver configuration.

The source and receivers are required to be located at the interface between two identical layers in the implementation (Bouchon, 2003). The position of the source and receiver can be anywhere within a layer; however, an artificial splitting of the layer is applied at the depth of the receiver or the source, i.e., splitting the layer into two identical layers with an interface at the depth of the source or receiver. The reflectivity method is easier to apply in this way. After the splitting, the source is located at the bottom of layer j , and the receiver is located at the top of layer m for the shallower-source-deeper-receiver situation.

In the following derivation, we use the P-SV system. For the SH system, the matrices and vectors are replaced with scalars. The overall amplitude vector $V_{1,2}^D$ for the down-going waves at the source depth is

$$\begin{aligned} V_{1,2}^D &= \begin{pmatrix} A_{1,2} \\ C_{1,2} \end{pmatrix} \\ &= (S_{1,2}^d + R^+ R^- S_{1,2}^d + R^+ R^- R^+ R^- S_{1,2}^d + \dots) \\ &\quad + (R^+ S_{1,2}^u + R^+ R^- R^+ S_{1,2}^u + R^+ R^- R^+ R^- R^+ S_{1,2}^u + \dots) \\ &= (I - R^+ R^-)^{-1} (S_{1,2}^d + R^+ S_{1,2}^u), \end{aligned} \quad (\text{A-1})$$

where R^+ and R^- are the reflectivities illustrated in Figure A-1; $S_{1,2}^d$ and $S_{1,2}^u$ are the source amplitude vectors; I is the identity matrix. $V_{1,2}^D$ takes all the reflections from the lower layers (first bracket) and the upper layers (second bracket) into consideration and, therefore, is the amplitudes of the *overall* down-going P- and SV-waves at the source depth. After the *overall* down-going amplitudes are obtained at the source level, we need to propagate them down through the

layers between the source and receiver by the overall down-going transmissivity matrix,

$$TT^D = F_{m-1} F_{m-2} \dots F_{j+1} F_j, \quad (\text{A-2})$$

where F_k characterizes the amplitude change through layer k and through the bottom interface of layer k . Note that for layer j there is no phase shifting through the phase matrix E_j in F_j , as the source is already located at the bottom of layer j after the artificial splitting. The overall down-going amplitudes at the receiver then are

$$V_{1,2}^{D,R} = \begin{pmatrix} A_{1,2}^R \\ C_{1,2}^R \end{pmatrix} = TT^D V_{1,2}^D, \quad (\text{A-3})$$

and the overall amplitudes of the upgoing waves at the receiver are related to the amplitudes of the downgoing waves by

$$V_{1,2}^{U,R} = \begin{pmatrix} B_{1,2}^R \\ D_{1,2}^R \end{pmatrix} = MT_m V_{1,2}^{D,R}, \quad (\text{A-4})$$

where MT_m is the local reflectivity matrix at the top of layer m . Combining the amplitudes $V_{1,2}^{U,R}$ and $V_{1,2}^{D,R}$ with the Green's functions calculated by the discrete wavenumber method (Bouchon, 2003) and integrating in the wavenumber and frequency domain, we can then obtain the analytic solution in a stratified medium where the receiver is deeper than the source.

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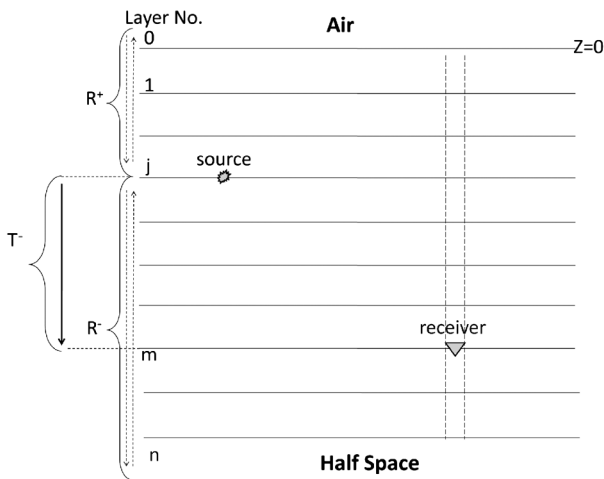


Figure A-1. Diagram of the reflectivity method for the deep borehole receiver configuration.

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